

# PROJECT 8 – NUMERICAL SIMULATION AND MODELLING

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Research Centre  
for Gas Innovation

cleaner energy for a sustainable future

3<sup>rd</sup> RCGI Workshop  
University of São Paulo, Brazil  
21 – 22 August 2018

# OPTIMIZATION AND STATISTICS IN ENERGY ECONOMICS

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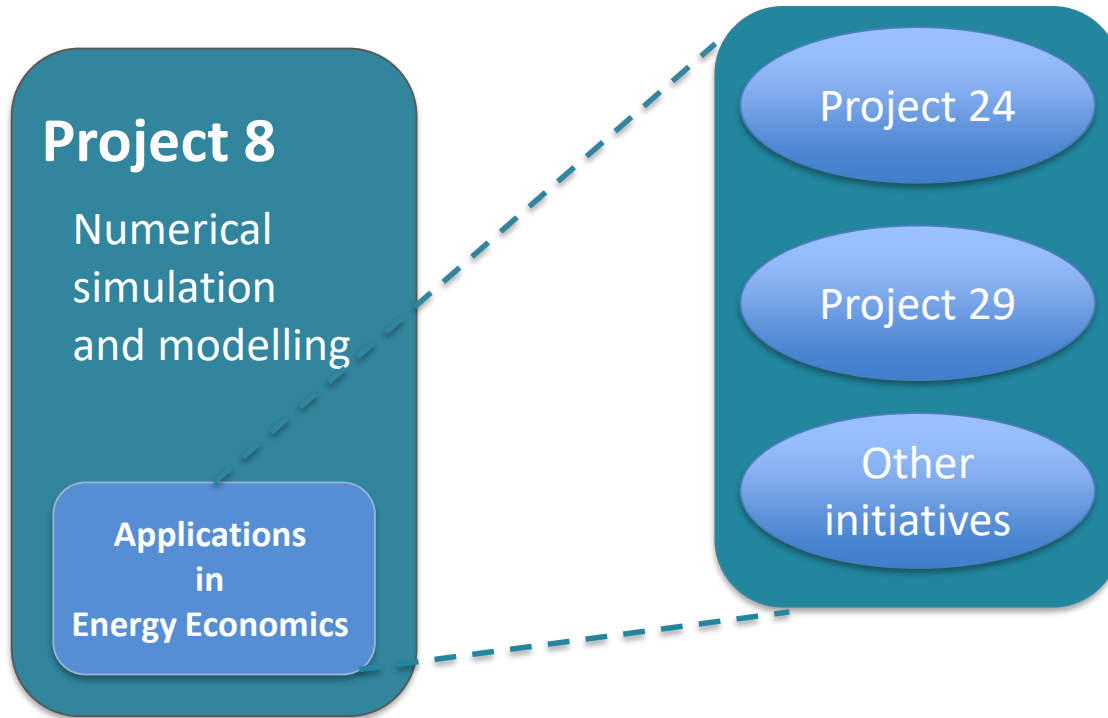


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# Collaboration with other projects



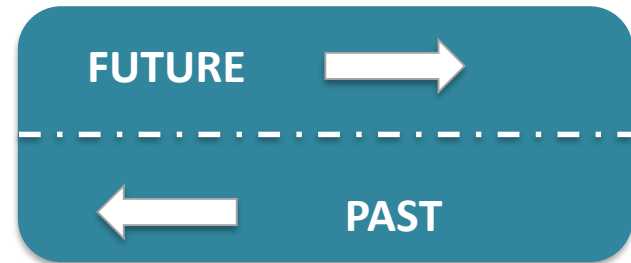
# Main purpose

- Development and applications of mathematical tools from optimization and statistics.

## Portfolio Models



## Forecasting Models



# Portfolio models



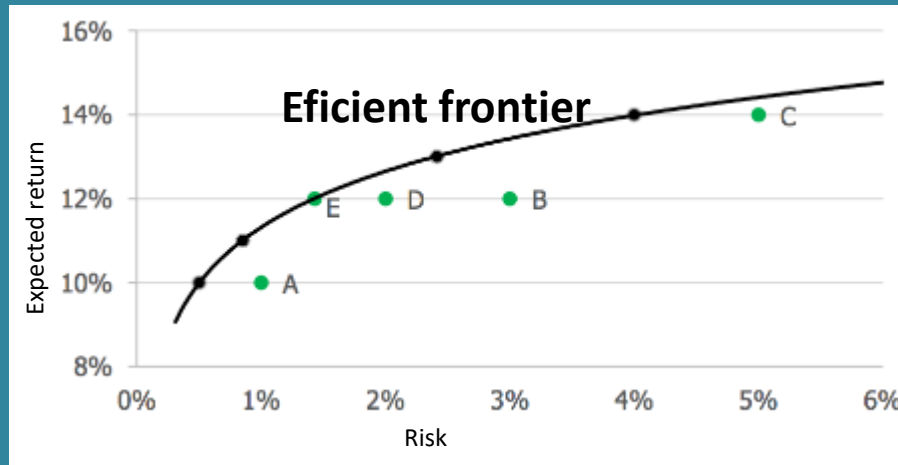
**RESOURCES**



**RISK**



**ASSETS**



## Portfolio Theory

Consolidated approach in finance theory

Consider trade-off risk/return

Portfolios on the efficient frontier are Pareto optimal

The investor chooses a portfolio according to her/his risk aversion

**The investor problem is a constrained optimization problem**

# Important application: Electricity Planning

**Technologies**

Oil

Wind

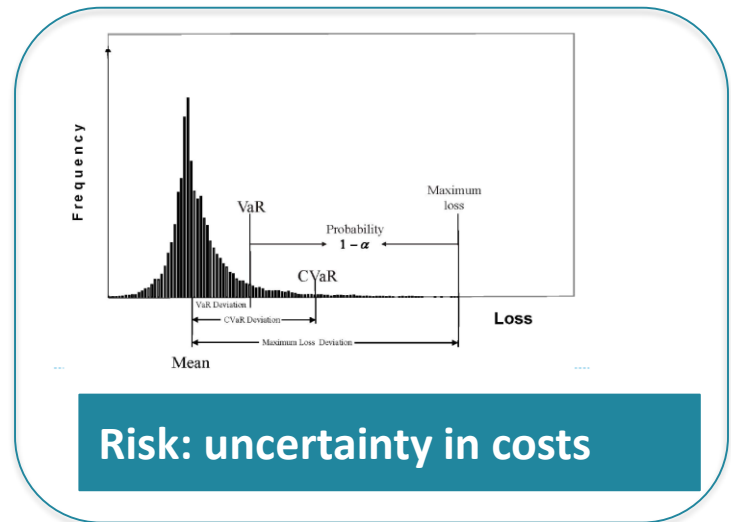
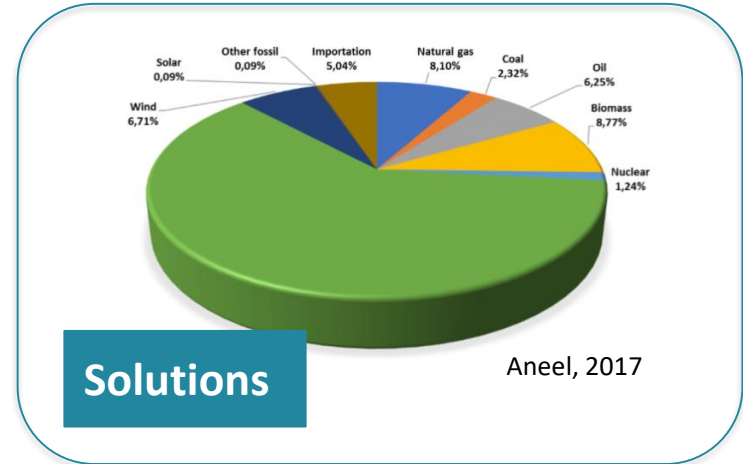
Coal

nuclear plants

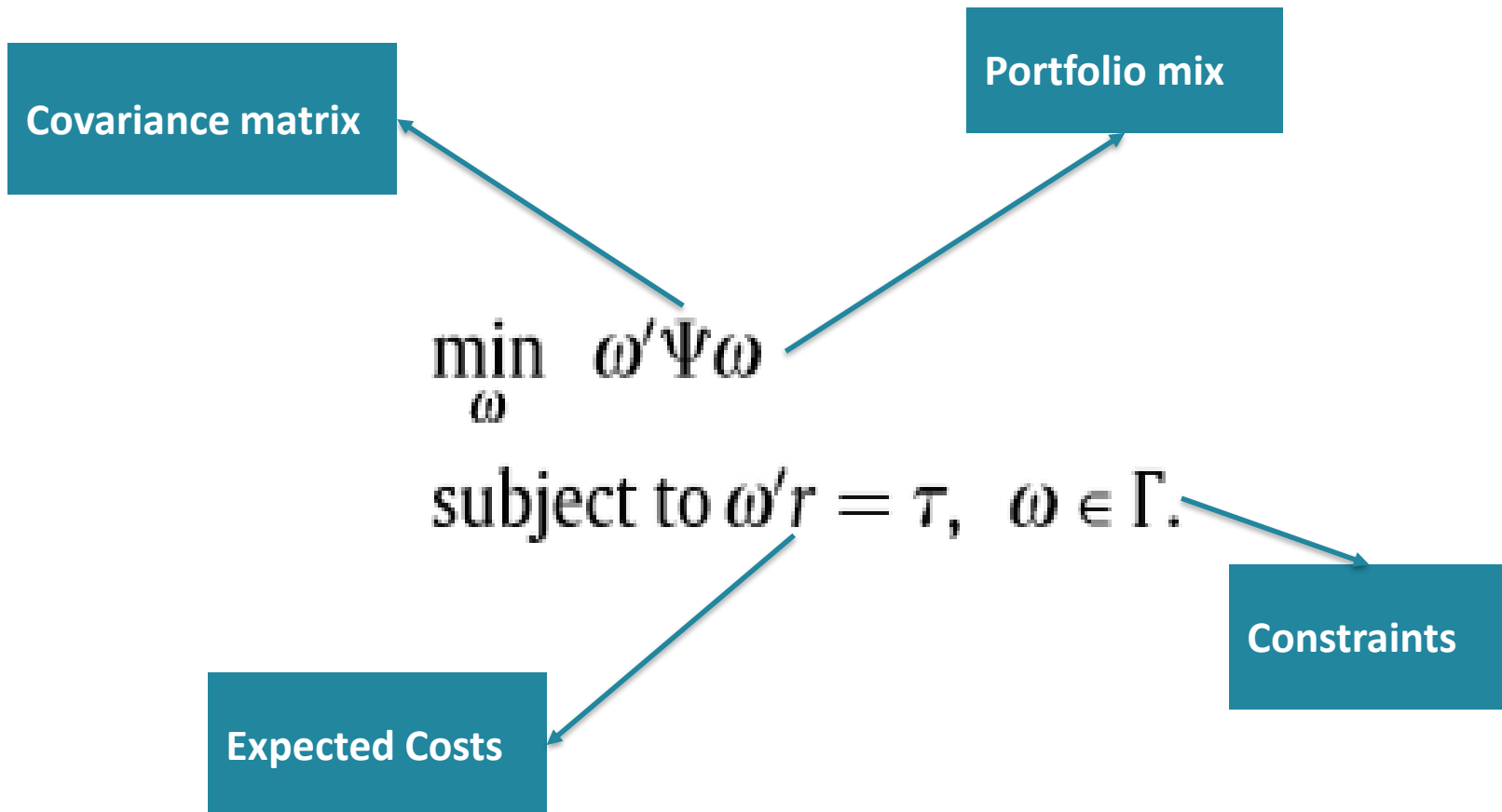
Biomass

Natural Gas

hydropower plants



- Traditional approach:





# Important application: Electricity Planning

## Challenge:

The consideration of the uncertainties associated with the future costs of technologies is crucial for planning purposes.

## Alternative approaches

### Robust optimization

Parameters inside an uncertainty set

$$\min_{\omega \in \Gamma} \max_{(r, \Psi) \in \mathcal{U}} (\omega' r + \lambda \omega' \Psi \omega).$$

### Bayesian optimization

Parameters are random variables with known probability distribution

$$\min_{\omega \in \Omega} \omega' \tilde{\mu} + \lambda \omega' \tilde{\Sigma} \omega.$$
$$C | \tilde{\mu}, \tilde{\Sigma} \sim t_{T-2N}(\tilde{\mu}, \tilde{\Sigma}), T-2N \geq 1 \quad \tilde{\mu} = \hat{\mu} \text{ and } \tilde{\Sigma} = \frac{(1+T^{-1})(T-1)}{T-2N-2} \hat{\Sigma}.$$

# Results: Robust Portfolio (Electricity)

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Energy Economics

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## Robust portfolio optimization for electricity planning: An application based on the Brazilian electricity mix



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Collaboration with Project 24

# Results: Robust Portfolio (Electricity)

**Table 6**  
Weights, exp. costs (cents USD/KWh), STD, CO<sub>2</sub> emission (TM/KWh) for Ref. 2024, optimal and robust mixes.

Fuel	Ref. 2024	Optimal	Poly. (Eq. (14))	Poly. (Eq. (16))	Box Eq. (27))	Ellip. Eq. (13))
Gas	10.96%	11.69%	12.25%	12.15%	5.87%	11.94%
Coal	1.7%	2.88%	1.54%	1.82%	1.53%	3.13%
Nuclear	1.7%	2.00%	2.00%	2.00%	2.00%	2.00%
Fuel oil	2.16%	2.42%	2.41%	2.41%	2.42%	2.41%
Biomass	9%	5.56%	5.57%	5.59%	5.56%	5.57%
Hydro	58.56%	55.72%	56.51%	56.78%	63.21%	60.17%
Wind	12%	14.00%	14.00%	13.53%	13.68%	9.05%
Small hydro	3.92%	5.73%	5.72%	5.72%	5.73%	5.73%
Exp. cost	7.155	7.155	7.155	7.153	7.155	7.155
Stand. dev	0.0420	0.0393	0.0451	0.0456	0.0495	0.0455
CO <sub>2</sub> emis.	0.0728	0.0879	0.0780	0.0802	0.0518	0.0912

**2024 Decennial Plan  
for Energy Expansion**

**Alternative uncertainty sets**

# Results: Robust Portfolio (Electricity)

Nominal data

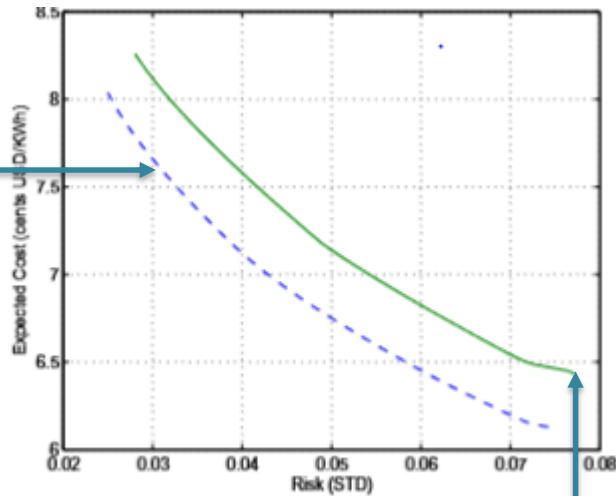


Fig. 2. Efficient frontier for the nominal data (dashed line) and the high CO<sub>2</sub> emission cost data (solid line).

Considering CO<sub>2</sub> costs  
Box uncertainty

Nominal data

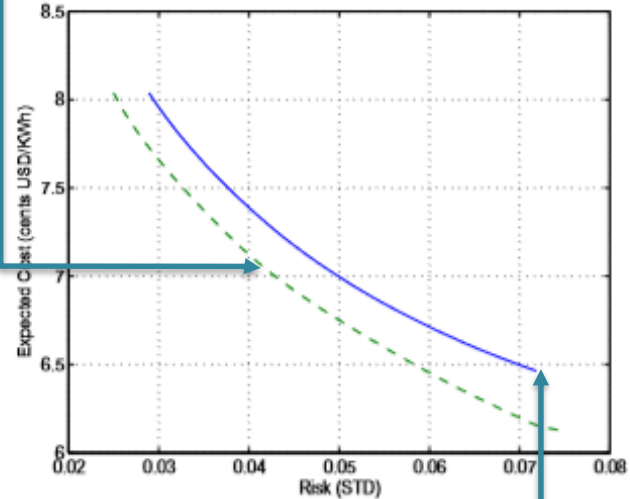


Fig. 3. Efficient frontier for the nominal data (dashed line) and the robust problem (13) with ellipsoidal uncertainty set for  $r$  (solid line).

Robust model  
Ellipsoidal uncertainty

# Results: Robust Portfolio (Biogas and bioelectricity)

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The insertion of biogas in the sugarcane mill product portfolio: A study using the robust optimization approach



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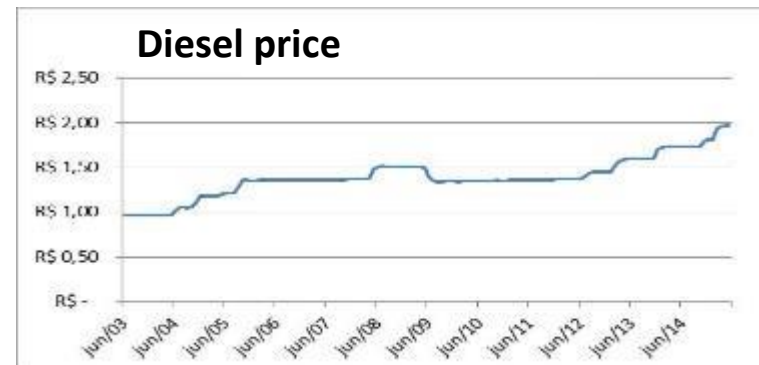
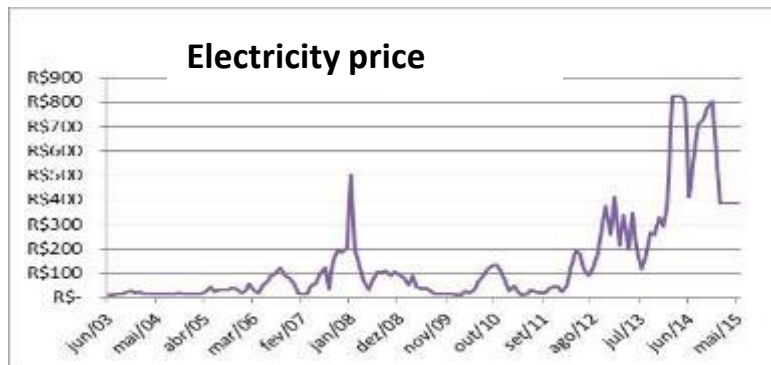
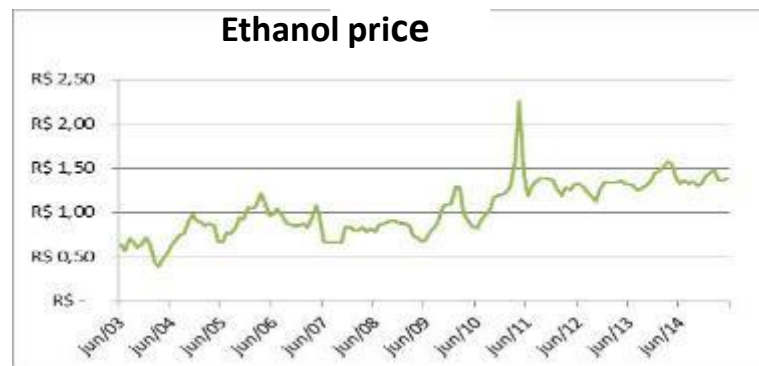
# Results: Robust Portfolio (Biogas and bioelectricity)

## Product portfolio- sugarcane industry

- Analysis of the economic impacts of biogas insertion in the **product mix** of sugarcane mills (ethanol, sugar, and electricity).
- A portfolio model was developed respecting all operational constraints (CVaR is the risk measure ).
- Uncertainties in the market prices
- Use of robust optimization techniques to mitigate the consequences of such price variations.

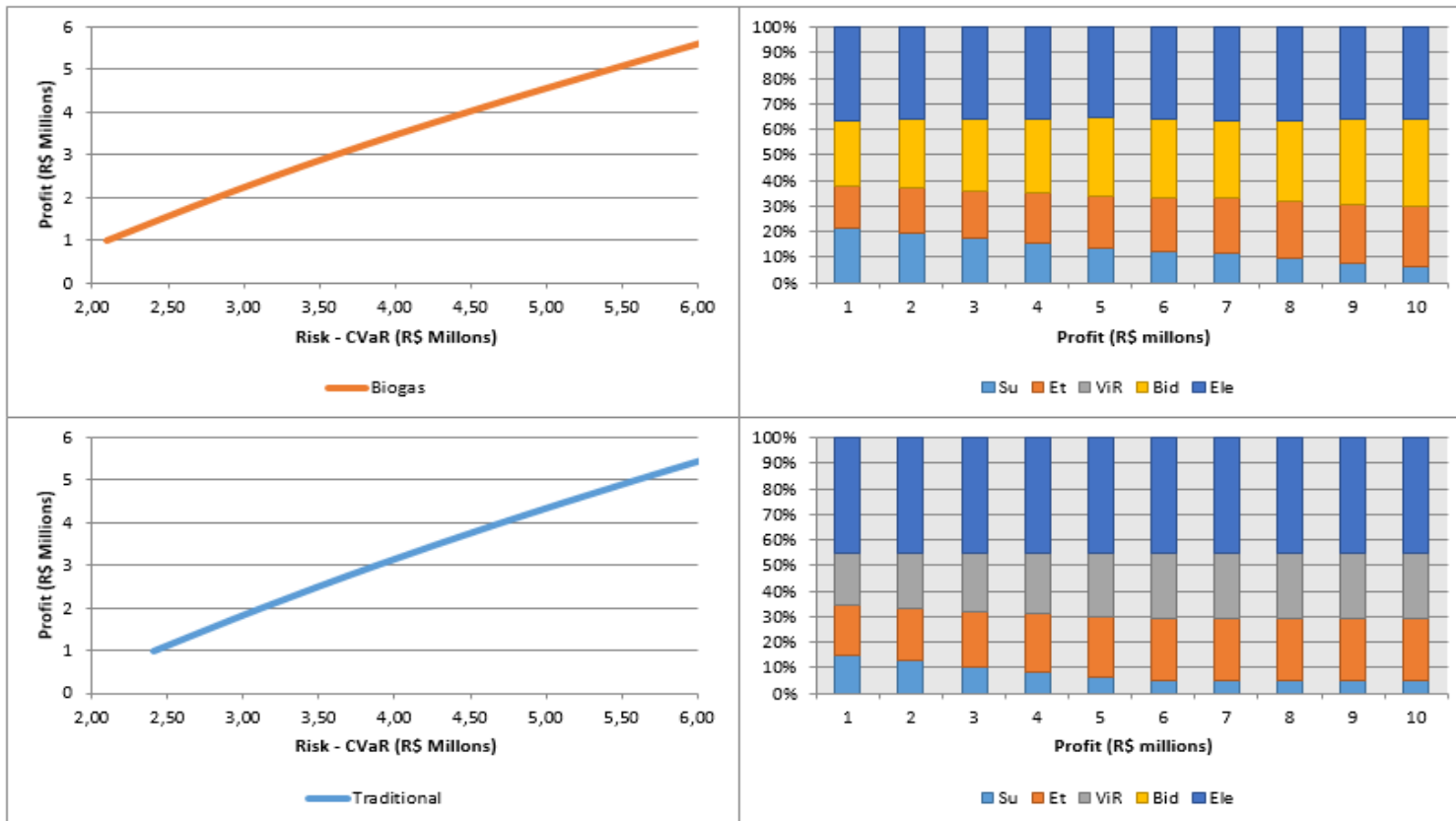
# Results: Robust Portfolio (Biogas and bioelectricity)

## Sugarcane industry: uncertainty on prices



# Results: Robust Portfolio (Biogas and bioelectricity)

## Efficient Frontiers and Portfolios





# Results: Bayesian Portfolio (Electricity)



Article

## Classical-Equivalent Bayesian Portfolio Optimization for Electricity Generation Planning <sup>†</sup>

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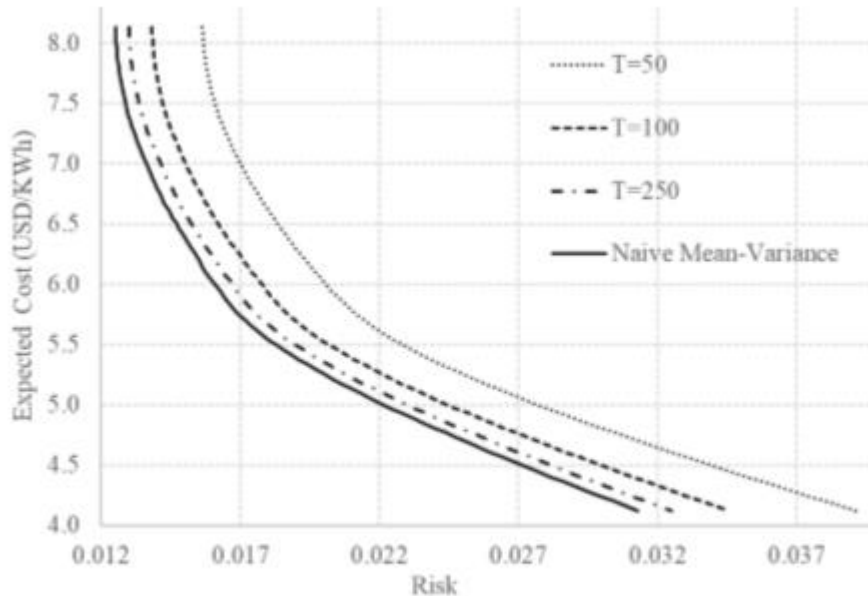
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<sup>†</sup> This paper is an extended version of our paper published in 37th International Workshop on Bayesian Inference and Maximum Entropy Methods in Science and Engineering, Jarinu, Brazil, 9–14 July 2017.

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# Results: Bayesian Portfolio (Electricity)

- The application of the approach was analyzed using improper and proper priors



## Improper priors

The investor has no information about the distribution of parameters

T is the number of historical observations

**Figure 1.** Efficient frontiers using naive and classical-equivalent Bayesian approaches for the improper prior case for some values of  $T$ .

# Results: Bayesian Portfolio (Electricity)

- The application of the approach was analyzed using improper and proper priors

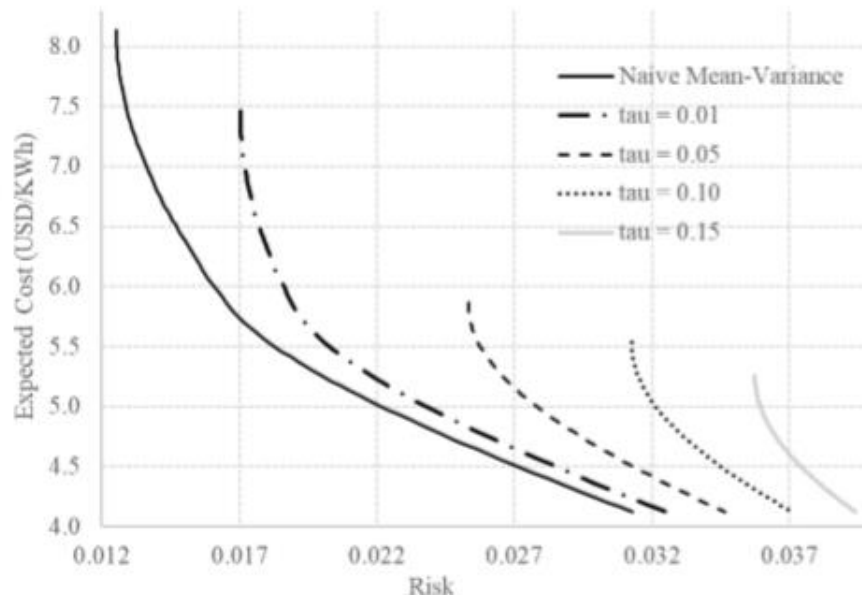


Figure 2. Efficient frontiers using naive and classical-equivalent Bayesian approaches for the proper prior case for some values of  $\tau$ .

## Proper priors

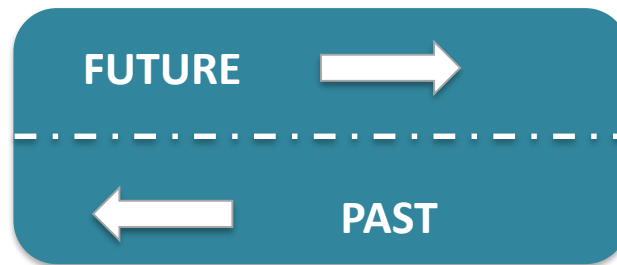
Specialists have informative beliefs about the mean and covariance of technology costs.

Tau represents the confidence strength the specialist places on the value of expected costs

$$\mu|\Sigma \sim N\left(\eta, \frac{1}{\tau}\Sigma\right), \Sigma \sim W^{-1}(\Psi, \nu),$$

expected costs based on the specialist experience

# Forecasting models



## Challenge:

The analysis of energy demand through statistical models

### Alternative approaches

Use and analysis of  
econometric models

Electricity Crisis

Price Elasticity

Improvement of  
econometric models

Short time series

Use of hybrid models

Gas for light vehicles

# Results: Analysis of Brazilian Electricity Crisis

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## Thermoelectric dispatch: From utopian planning to reality



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# Results: Analysis of Brazilian Electricity Crisis

Historically hydropower accounts for more than 80% of power generation in Brazil

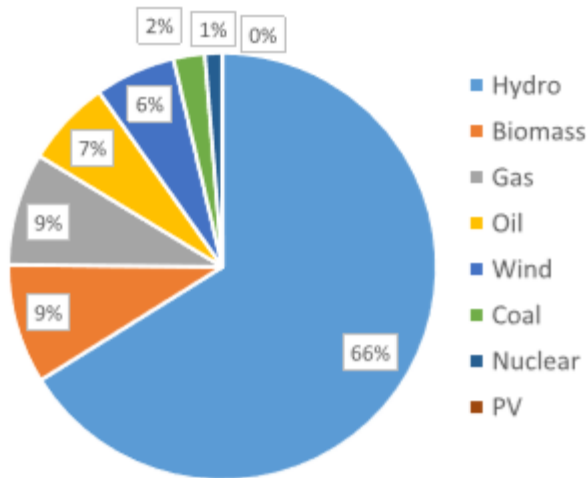


Fig. 1. Brazilian electricity matrix.  
Source: ANEEL (2016).



The lack of water in the reservoirs leads to serious crisis (e.g 2013-2015)

**Why???**

# Results: Analysis of Brazilian Electricity Crisis

- Thermoelectric dispatch

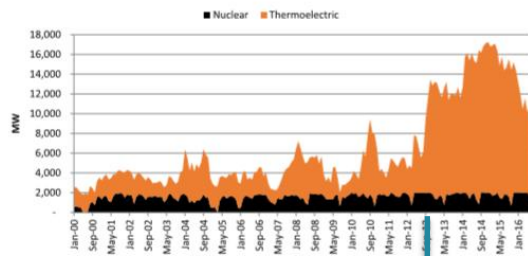


Fig. 4. Brazilian thermoelectric power generation. (For interpretation of the references to color in this figure, the reader is referred to the web version of this article.)  
Source: ONS, 2016.

2013

## Hypothesis regarding the causes

- divergence between the planning and execution of the expansion of power generation and transmission,
- the weakness of the NEWAVE dispatch software used by the government
- the below-average hydrology in 2014 and 2015.

Linear regression models were developed to forecast the electricity demand.

Specialists forecast of the hydroelectricity supply



# Results: Analysis of Brazilian Electricity Crisis

Demand forecast through linear models

(including seasonality, trend and dummies to represent the effect of crisis)

**Table 1**

Estimates of the coefficients (s.e. and p-values) of the regression model for the electricity demand of the industrial sector (Coefficient of determination  $R^2=0.94$ ).

Relevant Covariates for $Y_{1t}$ = the electricity demand of the industrial sector	Estimated coefficients	s.e.	p-Value
constant	-46650	10349	0.000
$X_1$ = the electricity fare of the industrial sector	20.08	1.99	0.000
$X_3$ = the electricity fare of the commercial sector	-16.31	2.09	0.000
$X_5$ = the population	374.2	66.0	0.000
$X_6$ = the per capita gross domestic product	-9.022	0.567	0.000
$X_8$ = the gross industrial product	0.152	0.013	0.000
$X_{11}$ = trend	-404.0	128.0	0.002
$X_{12}$ = effect of the Brazilian energy crisis	-565.0	210.0	0.008

**Table 2**

Estimates of the coefficients (s.e. and p-values) of the regression model for the electricity demand of the residential sector (Coefficient of determination  $R^2=0.98$ ).

Relevant Covariates for $Y_{2t}$ = the electricity demand of the residential sector	Coefficients	s.e.	p-Value
Constant	27,181	4050	0.000
$X_2$ = the electricity fare of the residential sector	-1.049	0.335	0.000
$X_5$ = the population	-137.5	25.8	0.000
$X_6$ = the per capita gross domestic product	1.43	0.19	0.000
$X_9$ = seasonality (cos)	232.2	24.0	0.000
$X_{11}$ = trend	533.2	52.2	0.000
$X_{12}$ = effect of the Brazilian energy crisis	-1656.5	84.5	0.000

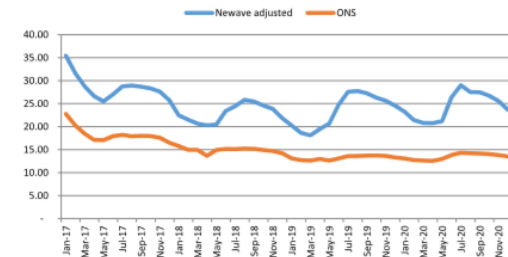
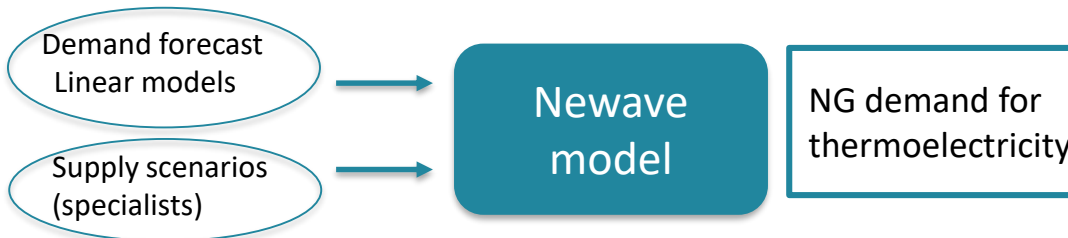
# Results: Analysis of Brazilian Electricity Crisis

**Table 3**  
Estimates of the coefficients (s.e. and p-values) of the regression model for the electricity demand of the commercial sector (Coefficient of determination  $R^2=0.98$ ).

Relevant Covariates for $Y_{3t}$ = the electricity demand of the commercial sector	Coefficients	s.e.	p-Value
Constant	3491	135	0.000
$X_3$ = the electricity fare of the commercial sector	-2.554	0.356	0.000
$X_9$ = seasonality (cos)	228.9	19.4	0.000
$X_{11}$ = trend	283.60	4.44	0.000
$X_{12}$ = effect of the Brazilian energy crisis	-737.1	72.6	0.000

**Table 4**  
Estimates of the coefficients (s.e. and p-values) of the regression model for the electricity demand of the other sectors (Coefficient of determination  $R^2=0.98$ ).

Relevant Covariates for $Y_{4t}$ = the electricity demand of other sectors	Coefficients	s.e.	p-Value
Constant	-17,800	1944	0.000
$X_5$ = the population	75.30	6.20	0.000
$X_6$ = the per capita gross domestic product	0.705	0.086	0.000
$X_7$ = the GINI index	14,148.0	1915.0	0.000
$X_9$ = seasonality (cos)	59.4	11.9	0.000
$X_{12}$ = effect of the Brazilian energy crisis	-471.7	42.2	0.000



**Fig. 22.** Projected natural gas consumption for thermal dispatch (million m3/day): ONS scenario versus sensitive analysis.  
Source: authors

# Next steps



(papers submitted)

Improvement of  
econometric models

Use of robust optimization in  
parameter estimation for linear models

Use of hybrid models

Use of hybrid models  
(econometric + Neural Networks) to  
GNV forecasting

# Next steps



(being studied)

Intentional sampling techniques

Apply Haphazard Intentional Sampling techniques to rationally re-engineer networks of measurement stations for atmospheric pollution and/or gas emissions

Hybrid and conventional vehicles for distribution in urban centers

With Project 29

Pre-salt Natural Gas for electricity generation

evaluate economic aspects of the generation of electricity from the natural gas from the Pre-salt, gas to wires versus Floating Liquefied Natural Gas (FLNG) technology for onshore generation



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**THANK YOU**



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